

Feel free to work with other students, but make sure you write up the homework and code on your own (no copying homework *or* code; no pair programming). Feel free to ask students or instructors for help debugging code or whatever else, though.

Note: You need to create a Github account for submission of the coding part of the homework. Please create a repository on Github to hold all your code and include your Github account username as part of the answer to the coding problems.

1 (1st fundamental form.) Compute the first fundamental form of a sphere at a point of the coordinate neighborhood given by the parametrization:

$$\mathbf{x}(\theta, \psi) = (\sin \theta \cos \psi, \sin \theta \sin \psi, \cos \theta).$$

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2 (Area.) Compute the area of the torus with the coordinate neighborhood corresponding to the parametrization:

$$\mathbf{x}(u, v) = ((a + r \cos u) \cos v, (a + r \cos u) \sin v, r \sin u), \quad 0 < u < 2\pi, 0 < v < 2\pi,$$

which covers the torus, except for a meridian and a parallel.

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3 (Coding.) Please use the 6 features (accelerometer: x, y, z and gyroscope: x, y, z) of H-MOG dataset to do the following:

(a) Pick some users. For each user pick 3 out of the 6 features. (Or if you have time, you can try all the 20 combinations.)

(b) For each data point of the 3 features v_1, v_2, v_3 , normalize the vector $\vec{v} = [v_1, v_2, v_3]$ by:

$$\hat{v} = \frac{\vec{v}}{\|\vec{v}\|_2}.$$

(c) Plot the normalized data points (vectors) on a sphere.

Note that a starter file is included under "resource" tab. Please feel free to ask TA if you have any question.

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